

# Kinetics of phase separation and thermal behaviour of gel-derived $\text{Al}_2\text{O}_3$ doped by $\text{Cr}_2\text{O}_3$ : an X-ray diffraction and fluorescence spectroscopy study

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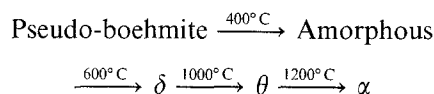
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Alpha-alumina crystallization from boehmite obtained from a gel was studied as a function of heating temperature and residence time. X-ray analysis allowed the determination of phases and their crystallite size; fluorescence spectroscopy was also studied as a complementary identification technique. The results reveal the general behaviour of gel-derived  $\text{Al}_2\text{O}_3$  phases and their transformation. The occurrence of an amorphous intermediate state was ruled out.

## 1. Introduction

The sol-gel route is a suitable approach to the synthesis of  $\text{Al}_2\text{O}_3$  for important applications such as the manufacture of basic products for high-value ceramics [1] and fibres [2–5]. Studies have shown that thermal treatment of the gel affords some irreversible phase transitions, a unique phase being associated with a definite temperature interval. The following scheme has been proposed to describe  $\text{Al}_2\text{O}_3$  gel evolution with temperature [6]:



This scheme refers to gel-derived  $\text{Al}_2\text{O}_3$  samples prepared with a single heating rate, disregarding possible effects of preparative details, ageing and phase stabilization for long-term treatments at intermediate temperatures.

In order to standardize the synthesis of  $\alpha$ -alumina by the gel method, it seems useful to have a more precise definition of the stability interval of the individual  $\text{Al}_2\text{O}_3$  phases by performing a systematic study of the behaviour of gel-derived  $\text{Al}_2\text{O}_3$  taking into account both heating temperature and residence time. The expectation is that some  $\text{Al}_2\text{O}_3$  phases may overlap their stability intervals owing to analogous thermodynamic contents, although their occurrence may involve different kinetics [7, 8].

The assessment of an amorphous phase as first product of pseudo-boehmite disappearance may also require a more detailed investigation. Indeed, the occurrence of this amorphous state may rule the kinetics of the entire process.  $\delta$ - $\text{Al}_2\text{O}_3$ ,  $\chi$ - $\text{Al}_2\text{O}_3$ ,  $\theta$ - $\text{Al}_2\text{O}_3$ , and  $\kappa$ - $\text{Al}_2\text{O}_3$  phases, observed at intermediate temperatures before  $\alpha$ - $\text{Al}_2\text{O}_3$  occurrence, may be derived from a single precursor leading to various  $\text{Al}_2\text{O}_3$  forms depending on crystallization conditions.

In addition, different gelling condition may afford different hydroxides which, as for natural aluminium hydroxides, may find variable intermediate phases before collapsing to  $\alpha$ - $\text{Al}_2\text{O}_3$  [9]. Thus, for better understanding of  $\text{Al}_2\text{O}_3$  crystallization it is promising to ascertain the occurrence and stability interval of the amorphous state, and the role of gel preparation procedures.

The present work uses wide-angle X-ray diffraction (XRD) analysis and optical fluorescence spectroscopy for phase characterization of  $\text{Cr}_2\text{O}_3$ -doped  $\text{Al}_2\text{O}_3$  gel.  $\text{Cr}^{3+}$  ion provide important coordination and structural information by means of fluorescence spectroscopy [10]. The combination of these techniques has recently been reported by Hirai *et al.* [6] in a study of gel-derived  $\text{Al}_2\text{O}_3$ ; our work extends that study with special attention to the kinetics of the crystallization processes. As a first approximation the role of  $\text{Cr}^{3+}$  in promoting alumina nucleation was disregarded; a further investigation on the possible influence of  $\text{Cr}^{3+}$  on preferential crystallization will be the object of a future study.

## 2. Experimental procedure

### 2.1. Preparation of samples by the sol-gel method and thermal treatment

Samples with 0.1 mol %  $\text{Cr}_2\text{O}_3$  were obtained by evaporation and calcination of an alumina sol. This sol was prepared as described by Yoldas [11]. In a typical experiment, aluminium iso-propoxide (100 g) and chromium acetylacetonate (0.17 g) were added to 400 ml of deionized  $\text{H}_2\text{O}$ . After heating for 1 h at  $80^\circ\text{C}$ , concentrated  $\text{HNO}_3$  (1.5 ml) was added; the system was left aside at  $100$  to  $110^\circ\text{C}$  for about one day. The reaction mixture was cooled to room temperature, producing a milky sol. The gel was then exchanged with water and subsequently dried at  $95^\circ\text{C}$ . This procedure had the effect of strongly reducing the

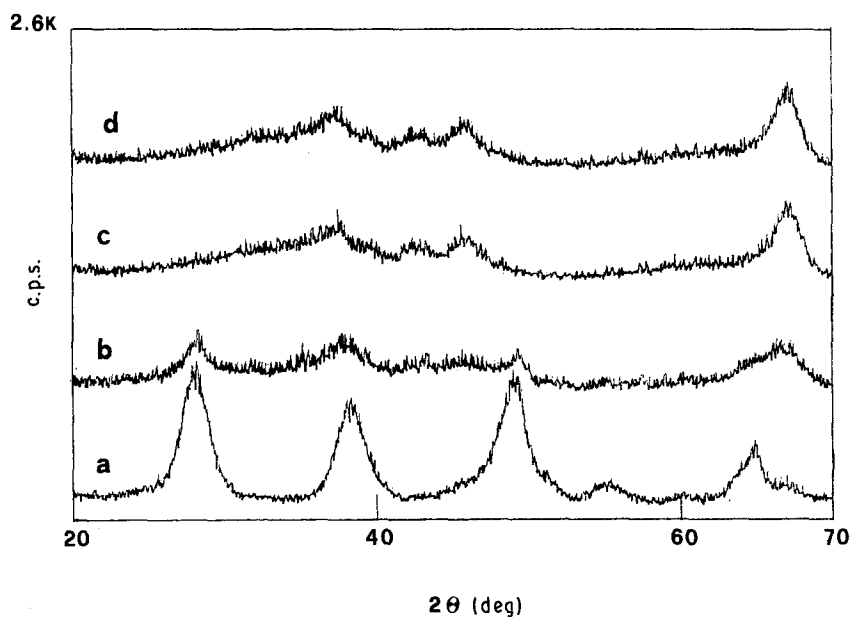


Figure 1 X-ray diffraction spectra of samples (a) AL 170, (b) AL 440, (c) AL 518 and (d) AL 600.

luminescence spectra of a broad-band contribution due to residual organic groups. The powders thus obtained were divided into various batches for successive ageing and thermal treatments. The samples were heated at  $4^{\circ}\text{C min}^{-1}$  up to various temperatures as reported in Table I. In some cases water-exchange was avoided, and samples were directly heated as previously described.

## 2.2. X-ray diffraction analysis

Powdered samples were examined in the reflection mode with a Rigaku D/max-B diffractometer with a scintillation counter and a graphite curved-crystal monochromator in the diffracted beam. Each measurement was carried out at  $1\text{ deg min}^{-1}$  with a step of  $0.02\text{ deg}$ , corresponding to  $1.2\text{ sec}$  per step. All samples were analysed at  $45\text{ kV}$  and  $40\text{ mA}$  in the range  $20^{\circ} \leq 2\theta \leq 70^{\circ}$ . A Casio 6000 computer was employed for data processing; besides the routine operation of background reduction, smoothing and peak-search, phase identification was carried out by means of a search-match program provided together with JCPDS cards [12]. Profile analysis was carried out for samples treated at  $1200^{\circ}\text{C}$ . Line-broadening analysis was performed following the Warren-Averbach method [13] applied to 012 and 024 peaks of  $\alpha\text{-Al}_2\text{O}_3$ , and employing a KCl sample as

standard for instrumental peak determination. For the other samples, where a complex overlap between peaks of the various phases occurred, the Scherrer formula was employed, together with a computer program for peak separation.

## 2.3. Fluorescence spectroscopy

Fluorescence spectra were taken by exciting with an HeNe or argon ion laser, emission being dispersed by a Jobin-Yvon HRS4 monochromator. Time-resolved spectra and lifetimes were recorded by mechanically chopping the laser light, which gave a time resolution of  $80\text{ }\mu\text{sec}$ . The excitation spectra were obtained by tungsten lamp plus monochromator excitation.

## 3. Results and discussion

The  $\text{Al}_2\text{O}_3$  gel was kept at  $170^{\circ}\text{C}$  for 24 h, ensuring the removal of solvent and organic radicals, as verified by means of differential thermal analysis. A weight loss between  $250$  and  $450^{\circ}\text{C}$ , corresponding to the virtually quantitative removal of  $\text{H}_2\text{O}$  from pseudo-boehmite, was found. Table I lists the samples examined and their thermal treatments.

Fig. 1 shows the X-ray spectrum evolution for samples treated for 2 h at temperatures in the range 170 to  $600^{\circ}\text{C}$ . This heating interval was monitored with particular care in order to determine the structural evolution of boehmite and the stability interval of a possible amorphous state. The product as prepared at  $170^{\circ}\text{C}$  shows the boehmite structure with an average dimension of crystallites of 5 nm. After 2 h at  $440^{\circ}\text{C}$  (Fig. 1b) the X-ray spectrum of the material was not suitable for immediate interpretation. Boehmite peaks were still recognizable but were weaker and broader than those observed for the product at  $170^{\circ}\text{C}$ . Other peaks may be attributed to microcrystallites of alumina phases other than boehmite. Peak broadness prevented definite phase identification, even for the sample kept at  $518^{\circ}\text{C}$  for 2 h (Fig. 1c), although the boehmite had completely disappeared. A tentative assignment to  $\delta\text{-Al}_2\text{O}_3$  and  $\chi\text{-Al}_2\text{O}_3$  is proposed: in the first case a good agreement is found between peak positions and relevant intensity ratios, whereas  $\chi\text{-Al}_2\text{O}_3$  occurrence

TABLE I Sample treatments

| Sample   | Temperature ( $^{\circ}\text{C}$ ) | Ageing time |
|----------|------------------------------------|-------------|
| AL 170   | 170                                | 12 h        |
| AL 440   | 440                                | 2 h         |
| AL 518   | 518                                | 2 h         |
| AL 518a  | 518                                | 5 min       |
| AL 518b  | 518                                | 12 h        |
| AL 600   | 600                                | 2 h         |
| AL 800   | 800                                | 2 h         |
| AL 800a  | 800                                | 5 min       |
| AL 800b  | 800                                | 12 h        |
| AL 1000  | 1000                               | 2 h         |
| AL 1200  | 1200                               | 2 h         |
| AL 1200a | 1200                               | 5 min       |
| AL 1200b | 1200                               | 20 min      |

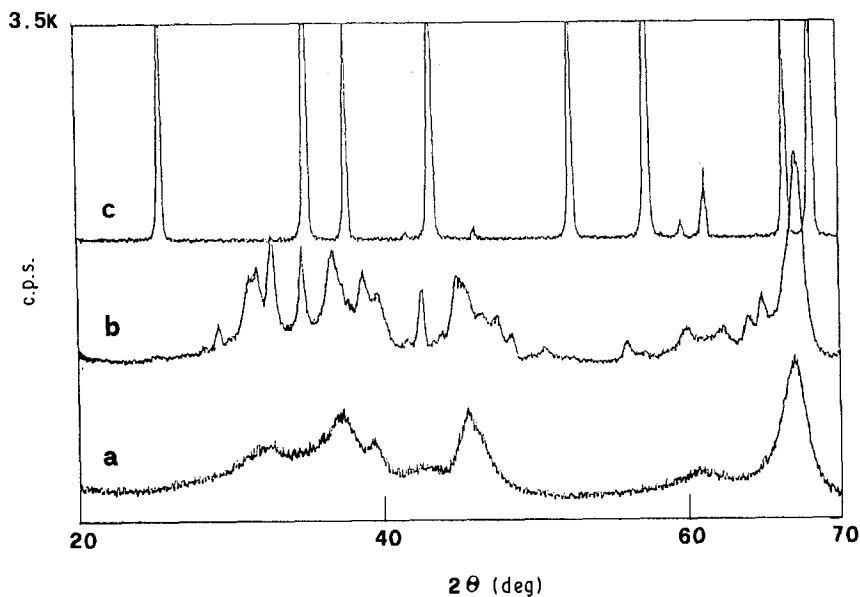


Figure 2 X-ray diffraction spectra of samples (a) AL 800, (b) AL 1000 and (c) AL 1200.

is supported by the presence of the peak at  $2\theta = 43^\circ$ . Among the aluminas stable at moderately low temperatures, only  $\chi$ - $\text{Al}_2\text{O}_3$  shows this peak. Prolonged heating at  $518^\circ\text{C}$  for 10 h or at  $600^\circ\text{C}$  for 2 h does not affect relevant X-ray spectra (Fig. 1d): the absence of any evolution with respect to the sample maintained at  $518^\circ\text{C}$  for only 2 h (Al 518) enlarges the field of coexistence between  $\chi$ - $\text{Al}_2\text{O}_3$  and  $\delta$ - $\text{Al}_2\text{O}_3$ . The complex overlapping of peaks attributable to the  $\chi$  and  $\delta$  phases is observed even for the sample heated at  $800^\circ\text{C}$  for 2 h (Fig. 2a). In this case more details are recognized because of peak sharpening, owing to better crystallization. On the other hand, the spectrum remains virtually unchanged on increasing the ageing time up to 12 h at the same temperature.

These data, collected for different ageing times in the interval  $440$  to  $800^\circ\text{C}$ , do not show any amorphous transition state produced by the disappearance of boehmite [6]; on the contrary our results can be accounted for by boehmite collapse to  $\delta$ - $\text{Al}_2\text{O}_3$  nucleation, followed by a moderate size increase upon further thermal treatments.

After a thermal treatment for 2 h at  $1000^\circ\text{C}$ , sample AL 1000 appeared to be constituted only of  $\theta$ - $\text{Al}_2\text{O}_3$ ,

and  $\kappa$ - $\text{Al}_2\text{O}_3$  (Fig. 2b): peak attribution is quite reliable owing to the good resolution, although (due to the background noise of the spectrum) nucleation of  $\alpha$ - $\text{Al}_2\text{O}_3$  or the residual presence of  $\delta$ - $\text{Al}_2\text{O}_3$  cannot be excluded. Actually, the presence of  $\alpha$ - $\text{Al}_2\text{O}_3$  nuclei was foreseen since  $\alpha$ - $\text{Al}_2\text{O}_3$  is detected by ageing at  $1000^\circ\text{C}$  for 10 h. Grain sizes determined according to the Scherrer approximation were 13 and 24 nm for  $\theta$ - $\text{Al}_2\text{O}_3$  and  $\kappa$ - $\text{Al}_2\text{O}_3$ , respectively. Heating at  $1200^\circ\text{C}$  for 2 h or for longer, up to 12 h, only produces  $\alpha$ - $\text{Al}_2\text{O}_3$  (Fig. 2c).

Samples not exchanged with water display different behaviour:  $\chi$ - and  $\kappa$ - $\text{Al}_2\text{O}_3$  phases were never observed, suggesting the invaluable effect of water content in determining the structural evolution of  $\text{Al}_2\text{O}_3$  gel.

The importance of residence time is evident on analysing the phase evolution occurring at  $1200^\circ\text{C}$ . Fig. 3 shows the spectra of samples prepared at  $1200^\circ\text{C}$  for different ageing times. After a few minutes at  $1200^\circ\text{C}$  (Fig. 3a) the detectable phase is  $\delta$ - $\text{Al}_2\text{O}_3$ , but a 20 min ageing is sufficient to modify the microstructure with the formation of  $\alpha$ -,  $\theta$ - and  $\kappa$ - $\text{Al}_2\text{O}_3$  (Fig. 3b). At this stage the contribution of  $\alpha$ - $\text{Al}_2\text{O}_3$  is the most important, although the crystallite size is

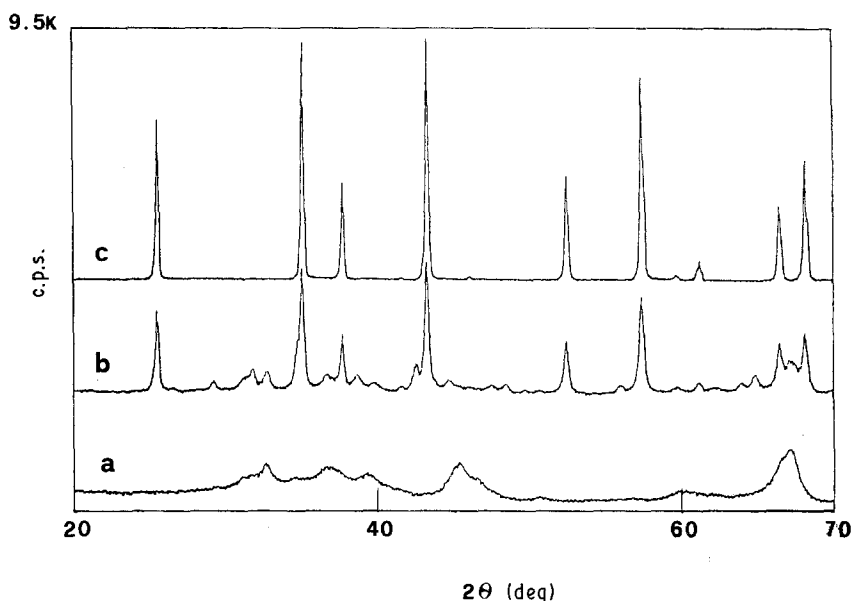


Figure 3 X-ray diffraction spectra of samples (a) AL 1200b, (b) AL 1200c and (c) AL 1200.

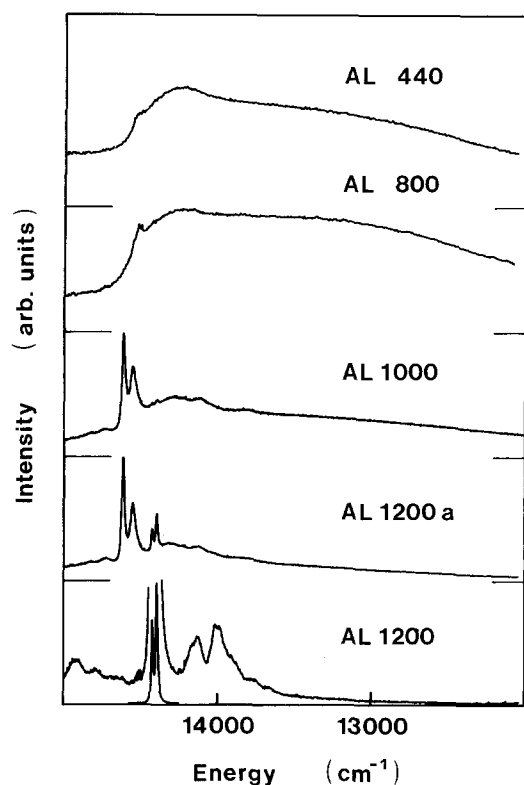


Figure 4 Room-temperature emission spectra of several samples under 632.8 nm excitation. Traces are labelled following Table I. The intensity of the doublet (lower trace) was divided by a factor of 20.

smaller than for the sample heated for 2 h (Fig. 3c). The evaluation of crystallite dimensions for samples treated at 1200°C for 20 min (AL 1200b) and 2 h (AL 1200) was performed by the Scherrer and Warren–Averbach approaches. In the absence of well-shaped pure crystalline standards of  $\chi$ -,  $\theta$ -, and  $\kappa$ -Al<sub>2</sub>O<sub>3</sub>, only the crystallite dimensions of  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> were measured and compared; the values obtained are reported in Table II. The agreement of the results is worthy of note, taking into account that the Scherrer formula is expected to give overestimated values, especially for well crystallized and slightly strained systems.

Most samples identified by X-ray analysis were studied by fluorescence spectroscopy. Fig. 4 shows the room-temperature fluorescence spectra under 623.8 nm excitation for the set of samples heated for 2 h at different temperatures. Sample AL 1200, aged for 2 h at 1200°C, shows the characteristic emission spectrum of ruby (chromium-doped  $\alpha$ -alumina) in agreement with X-ray results. The spectrum is dominated by R1 and R2 lines arising from the transition from the first excited level <sup>2</sup>E, split by 29 cm<sup>-1</sup> in the case of trigonal distortion [14, 17], to the ground state <sup>4</sup>A<sub>2</sub>. In addition to the R-zero phonon lines, weaker structures due to their relative sidebands may also be observed.

TABLE II Mean dimension of crystallites of  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> heated at 1200°C for 20 min and 2 h

| Calculation method | Mean dimension (nm) |         |
|--------------------|---------------------|---------|
|                    | AL 1200b            | AL 1200 |
| Warren–Averbach    | 60                  | 110     |
| Scherrer           | 90                  | > 200   |

As regards samples prepared at lower temperatures, direct assignment of the observed luminescences is not possible since, to our knowledge, the spectroscopy of Cr<sup>3+</sup> ions in alumina phases other than  $\alpha$  has never been studied in detail. However, comparison of the spectra offers valuable evidence of structural evolution.

For annealing temperatures in the range 400 to 800°C the luminescence spectrum consists of broad, featureless bands extending from 14 500 to 12 000 cm<sup>-1</sup>. At higher annealing temperatures, several structures appear and broad-band contributions decrease. All the observed features are due to Cr<sup>3+</sup> luminescence, as can be verified from their excitation spectra characterized by two strong bands arising from the <sup>4</sup>A<sub>2</sub> → <sup>4</sup>T<sub>2</sub> and <sup>4</sup>A<sub>2</sub> → <sup>4</sup>T<sub>1</sub> Cr<sup>3+</sup> transitions in octahedral environments.

The broad band extending down to 12 000 cm<sup>-1</sup>, which decreases in intensity on increasing the annealing temperature, is short-lived (lifetime < 0.1 m sec). On the contrary the structures between 14 500 and 14 000 cm<sup>-1</sup>, which gain intensity on increasing the annealing temperature, are sharper and long-lived (lifetime in the 1 to 9 m sec range). The observation of broad bands together with sharp structures with different lifetimes is not surprising. In octahedral coordination the ground state of Cr<sup>3+</sup> is <sup>4</sup>A<sub>2</sub>, while the first excited state may be <sup>2</sup>E or <sup>4</sup>T<sub>2</sub> depending on the strength of the crystal field. According to the diagrams of Tanabe and Sugano [16, 17] the <sup>2</sup>E excited state is weakly affected by the crystal field and the <sup>2</sup>E → <sup>4</sup>A<sub>2</sub> transition is a sharp zero phonon line and has phonon satellites. The <sup>4</sup>A<sub>2</sub> → <sup>2</sup>E transition is spin-forbidden but is partially allowed by <sup>2</sup>E–<sup>4</sup>T<sub>2</sub> spin-orbit mixing and its lifetime may be very long (tens of milliseconds). At weak crystal field, the <sup>4</sup>T<sub>2</sub> level may be lower in energy than <sup>2</sup>E so that fluorescence is due to the spin-allowed <sup>4</sup>T<sub>2</sub> → <sup>4</sup>A<sub>2</sub> transition; this is a broad vibronic band extending to the near infrared, with a lifetime of the range of tens to hundreds of microseconds.

In a disordered system, the whole of the above situation may be found at different sites. For example, in glasses [18, 19] the <sup>2</sup>E → <sup>4</sup>A<sub>2</sub> emission line is observed together with a <sup>4</sup>T<sub>2</sub> → <sup>4</sup>A<sub>2</sub> broad band peaked at lower energies and deriving from weak crystal-field centres. The <sup>2</sup>E → <sup>4</sup>A<sub>2</sub> line is broadened by disorder and shows a wide distribution of lifetimes. The contribution of ions in different sites can thus be selected by means of time-resolved spectroscopy or selective excitation.

In this regard, the emission of samples AL 440 and AL 800 (Fig. 4) is found to be composed of a broad <sup>2</sup>E structure around 14 200 cm<sup>-1</sup>, whose excitation spectrum is characteristic of a high crystal field and very distorted centres, as usually observed in highly disordered systems. On the other hand, in these samples low crystal-field centres also occur. In fact, in the excitation spectra of the low-energy tail of the emission at about 12 500 cm<sup>-1</sup>, where lifetimes less than 0.1 m sec are measured, the <sup>4</sup>T<sub>2</sub> excitation band is very broad and shifted towards low energies. The <sup>4</sup>T<sub>2</sub> low-energy tail extends below 14 000 cm<sup>-1</sup> in the <sup>2</sup>E region, indicating that, for these Cr<sup>3+</sup> ions, the <sup>4</sup>T<sub>2</sub> level is the first excited one.

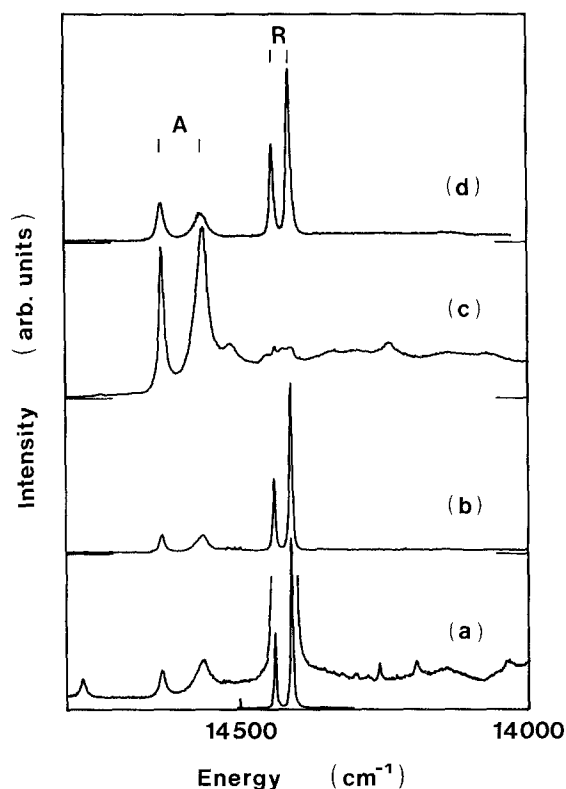


Figure 5 Details of emission spectra in the energy range of R and A lines at 77 K: (a) sample AL 1200; (b) sample AL 1200b; (c, d) sample AL 1200a. Excitation line: 632.8 nm for spectra (a), (b) and (c); 514.5 nm for spectrum (d). The intensity of the doublet (lower trace) was divided by a factor of 20.

Samples AL 1000 AL 1200a show sharp, long-lived features in their emission spectra (Fig. 4), assigned to  $\text{Cr}^{3+}$  ions in high crystal-field sites as verified by excitation spectroscopy. At the present time we cannot attempt assignment of the observed chromium-related emission to definite sites of definite transition-alumina phases.

Fig. 5 shows in detail the last steps of crystalline evolution towards the  $\alpha$ -phase. The major features of all spectra in Fig. 5 are the two doublets A and R. By increasing either annealing temperature or heating time, the R lines of  $\alpha$ -alumina gradually increase, being practically the only observable feature in the emission spectra (Fig. 5a). The A doublet arises from a site in a phase different than that of  $\alpha\text{-Al}_2\text{O}_3$ . It dominates the spectrum (Fig. 5c) and gradually disappears with ageing at 1200°C.

The level of sensitivity which can be attained in a fluorescence measurement in detecting the presence of very diluted phases is also shown in Fig. 5. For instance, in the X-ray spectrum of sample AL 1200 only the  $\alpha$ -phase is detected (Fig. 3c), while in Fig. 5a the A lines still occur, indicating that complete crystallization in the  $\alpha$ -phase has not yet taken place. This fact underlines the much higher analytical power of spectroscopic analysis in comparison with X-ray phase identification. Moreover, the analytical power of optical spectroscopy can be increased since by varying the excitation line, the sensitivity to the emission of an individual phase may be increased. This is shown in Figs 5c and d where a drastic variation in the relative intensity of the A and R doublets is obtained only by changing the exciting line from 632.8 to 514.5 nm,

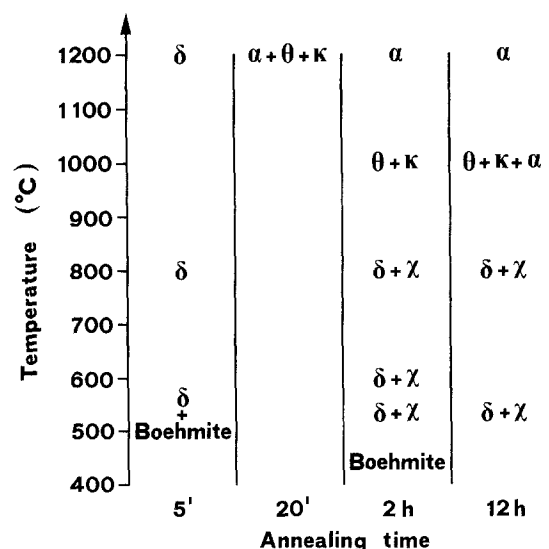


Figure 6 Diagram of  $\text{Al}_2\text{O}_3$  phases, for  $\text{H}_2\text{O}$ -exchanged samples, at various temperatures and times.

respectively. With this same experimental method we also observed nucleation of  $\alpha$ -alumina in sample AL 1000, heated for 2 h at 1000°C (Fig. 4). The identification of this phase is based on the appearance, in the emission spectrum under 514.5 nm excitation, of weak but detectable R-lines of chromium in  $\alpha$ -alumina. It is worthy of note that, for the same sample, X-ray data give a structure composed only of  $\theta$ - and  $\kappa\text{-Al}_2\text{O}_3$  (Fig. 2b).

Fluorescence spectroscopy can be used as a complementary method for crystallite size analysis. Thus, the linewidth of the R-lines at 77 K decreases with increasing annealing temperature (Table III). After 2 h at 1200°C (AL 1200) the width of the R lines is roughly a factor of two larger than in ruby crystals of the same chromium concentration. The larger linewidth reflects the presence of an important degree of disorder on the  $\text{Cr}^{3+}$  sites in  $\alpha$ -alumina. The narrowing of the R lines with annealing may be due to size effects. A progressive increase in the average crystalline size, as observed by X-ray analysis (Table II), should reduce grain-surface effects: in fact, the grain surface is seen as a defect by the neighbouring chromium impurities.

As regards the linewidths of the A lines (Table III), a decrease is observed on going from 1000 to 1200°C. However, longer treatments at 1200°C with progressive growth of the  $\alpha$  phase do not cause any further narrowing. Since A lines are associated with an  $\text{Al}_2\text{O}_3$  phase different from  $\alpha$ -alumina, these results confirm the possible presence at 1200°C of phases other than  $\alpha\text{-Al}_2\text{O}_3$ : indeed, a broadening is observed in sample

TABLE III Full-width-half-maximum (FWHM) of R and A lines at 77 K

| Sample   | FWHM ( $\text{cm}^{-1}$ )* |                     |                     |                     |
|----------|----------------------------|---------------------|---------------------|---------------------|
|          | $\Gamma(\text{R1})$        | $\Gamma(\text{R2})$ | $\Gamma(\text{A1})$ | $\Gamma(\text{A2})$ |
| AL 1000  | —                          | —                   | 55                  | 16                  |
| AL 1200a | 7                          | 7                   | 23                  | 10                  |
| AL 1200b | 5                          | 5                   | 21                  | 10                  |
| AL 1200  | 4                          | 4                   | 25                  | 11                  |

\*R1, 14 418  $\text{cm}^{-1}$ ; R2, 14 447  $\text{cm}^{-1}$ ; A1, 14 572  $\text{cm}^{-1}$ ; A2, 14 642  $\text{cm}^{-1}$ .

AL 1200, where there are very few domains still not crystallized as the  $\alpha$ -phase.

#### 4. Conclusion

In conclusion, our results indicate that an intermediate amorphous state cannot be proposed for the pseudo-boehmite transformation to  $\text{Al}_2\text{O}_3$ , which involves the possible occurrence of various crystalline phases. Taking into account the heating temperatures and residence times, the resulting picture of  $\text{Al}_2\text{O}_3$  phases obtained is shown in Fig. 6. This general scheme may be further complicated by the experimental preparation procedure: water content was found to favour the appearance of  $\chi$  and  $\kappa$  phases for temperatures in the range 440 to 1000°C.

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